

Reducerea la primul cadran:

$$\text{II}-\text{I}: \sin(\pi - x) = \sin x; \cos(\pi - x) = -\cos x; \operatorname{tg}(\pi - x) = -\operatorname{tg} x$$

$$\text{III}-\text{I}: \sin(\pi + x) = -\sin x; \cos(\pi + x) = -\cos x; \operatorname{tg}(\pi + x) = \operatorname{tg} x$$

$$\text{IV}-\text{I}: \sin(2\pi - x) = -\sin x; \cos(2\pi - x) = \cos x; \operatorname{tg}(2\pi - x) = -\operatorname{tg} x$$

$$\cos -x = \cos x; \sin -x = -\sin x$$

Formule trigonometrice pentru suma si diferența :

$$\cos(a+b) = \cos a \cos b - \sin a \sin b$$

$$\sin(a+b) = \sin a \cos b + \cos a \sin b$$

$$\operatorname{tg}(a+b) = \frac{\operatorname{tg} a + \operatorname{tg} b}{1 - \operatorname{tg} a \operatorname{tg} b}$$

$$\cos(a-b) = \cos a \cos b + \sin a \sin b$$

$$\sin(a-b) = \sin a \cos b - \cos a \sin b$$

$$\operatorname{tg}(a-b) = \frac{\operatorname{tg} a - \operatorname{tg} b}{1 + \operatorname{tg} a \operatorname{tg} b}$$

Functii trigonometrice cu \neq complementare:

$$\cos\left(\frac{\pi}{2} - a\right) = \sin a; \operatorname{tg}\left(\frac{\pi}{2} - a\right) = \operatorname{ctg} a$$

$$\sin\left(\frac{\pi}{2} - a\right) = \cos a; \operatorname{ctg}\left(\frac{\pi}{2} - a\right) = \operatorname{tg} a$$

Functii trigonometrice cu \neq suplementare:

$$\cos(\pi - a) = -\cos a; \operatorname{tg}(\pi - a) = -\operatorname{tg} a$$

$$\sin(\pi - a) = \sin a; \operatorname{ctg}(\pi - a) = -\operatorname{ctg} a$$

Functii trigonometrice ale \neq dublu:

$$\cos 2x = \cos^2 x - \sin^2 x = 1 - 2 \sin^2 x = 2 \cos^2 x - 1$$

$$\sin 2x = 2 \sin x \cos x; \operatorname{tg} 2x = \frac{2 \operatorname{tg} x}{1 - \operatorname{tg}^2 x}$$

Functiile trigonometrice ale unu \neq in functie de cos dublului sau:

$$\cos^2 x = \frac{1 + \cos 2x}{2} \Rightarrow \cos x = \pm \sqrt{\frac{1 + \cos 2x}{2}}; \sin^2 x = \frac{1 - \cos 2x}{2} \Rightarrow \sin x = \pm \sqrt{\frac{1 - \cos 2x}{2}}$$

$$\operatorname{tg}^2 x = \frac{1 - \cos 2x}{1 + \cos 2x} \Rightarrow \operatorname{tg} x = \pm \sqrt{\frac{1 - \cos 2x}{1 + \cos 2x}}$$

Transformarea sumelor in produs:

$$\sin \alpha \pm \sin \beta = 2 \sin \frac{1}{2}(\alpha \pm \beta) \cos \frac{1}{2}(\alpha \mp \beta)$$

$$\cos \alpha \pm \cos \beta = 2 \cos \frac{1}{2}(\alpha + \beta) \cos \frac{1}{2}(\alpha - \beta)$$

Transformarea produselor in sume:

$$\cos \alpha * \sin \beta = \frac{\cos(\alpha + \beta) + \cos(\alpha - \beta)}{2}; \sin \alpha * \sin \beta = \frac{\cos(\alpha - \beta) - \cos(\alpha + \beta)}{2}; \sin \alpha * \cos \beta = \frac{\sin(\alpha + \beta) + \sin(\alpha - \beta)}{2}$$

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